

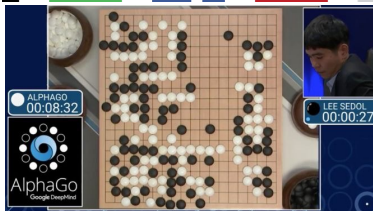
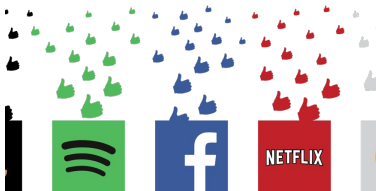
Active Sensing via Learning

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Question: Assume that the variance of the first n natural numbers is 30, and the variance of the first m even natural numbers is 16. Compute $m + n$.

Model output: Let σ^2 be the variance of the first n even natural numbers, and σ'^2 be the variance of the first m natural numbers. Then, we have $\sigma'^2 = \frac{n^2-1}{12}$ and $\sigma^2 = \frac{m^2-1}{3}$. We solve the system of equations:

$$\begin{aligned}\frac{n^2-1}{12} &= 10 \\ \frac{m^2-1}{3} &= 16.\end{aligned}$$

This translates into the system

$$\begin{aligned}n^2 &= 121 \\ m^2 &= 49 + 1 = 48.\end{aligned}$$

Therefore, $n = \boxed{11}$ and $m = \boxed{7}$, so $n + m = \boxed{18}$.

Question: For every $a, b, h \neq 0$ prove that

$$\frac{a^2 + b^2}{2} > \left(\frac{a+b}{2}\right)^2.$$

Model output:

$$\begin{aligned}\frac{a^2+b^2}{2} &> \left(\frac{a+b}{2}\right)^2 \\ \Leftrightarrow \frac{a^2+b^2}{2} &> \frac{a^2+2ab+b^2}{4} \\ \Leftrightarrow a^2 + b^2 &> \frac{a^2+2ab+b^2}{2} \\ \Leftrightarrow 2a^2 + 2b^2 &> a^2 + b^2 + 2ab \\ \Leftrightarrow a^2 + b^2 &> 2ab \\ \Leftrightarrow a^2 + b^2 - 2ab &> 0 \\ \Leftrightarrow (a-b)^2 &> 0\end{aligned}$$

which is true, because the square of a real number is positive.

- Why are neural networks so powerful?
 - **Universal** functional mapping by pattern matching;
 - Design neural network architectures to explore the **problem structure**;
 - Incorporating **vast** amount of data and problem instances;
 - **Highly parallel and scalable** implementation.
- What are the roles of machine learning for wireless communications?

- The fundamental limits of communications are governed by information theory.
- Channel capacity is the maximum mutual information, which is a function of the channel $p(y|x)$ and the input distribution $p(x)$:

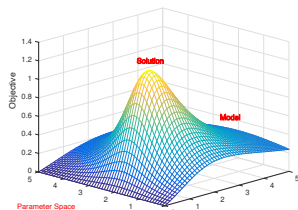
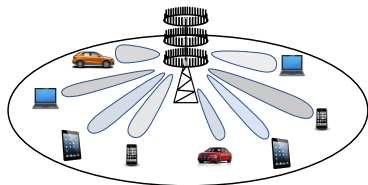
$$C = \max_{p(x)} I(X; Y).$$

- The overall communication problem can be broken down into the following parts:
 - Use source coding to convert the source into bits.
 - Use pilots to estimate the channel $p(y|x)$.
 - Use adaptive modulation, beamforming, power control for optimizing $p(x)$.
 - Use channel coding to transmit the bits.

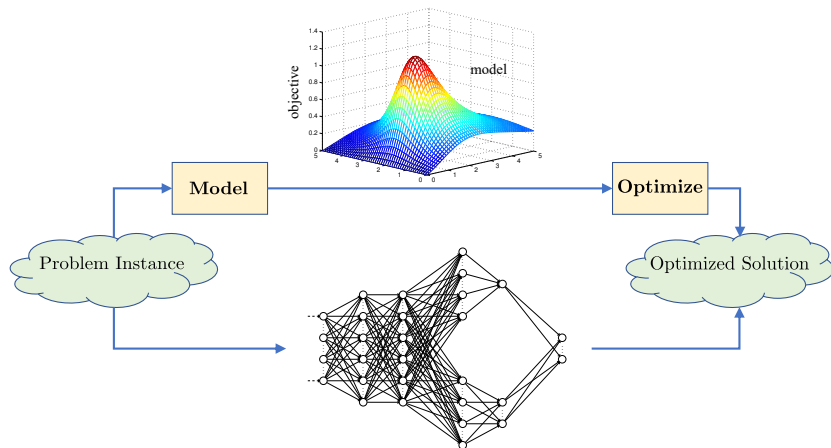


- The traditional communication system design paradigm is *model-based*.

- Channel estimation requires assumption on the model:
 - More parameters make model more accurate, but makes model harder to estimate.
 - Longer pilot makes estimation easier but consumes valuable coherence time/bandwidth.
 - Loss function for channel estimation is typically arbitrary (e.g., square-error).
 - There is no universal theory about which model is the most suitable.
- Mathematical optimization requires precise problem formulation:
 - The same problem can be parameterized in many different ways.
 - The holy grail of optimization is to transform a problem into convex form.
 - There is no universal theory about how to best transform the optimization landscape.



Role of Machine Learning in Wireless Air Interface



- This Talk: [A Data-Driven Approach to Communications and Sensing](#)

Learn to Beamform

- How to obtain channel state information (CSI) for massive MIMO systems?

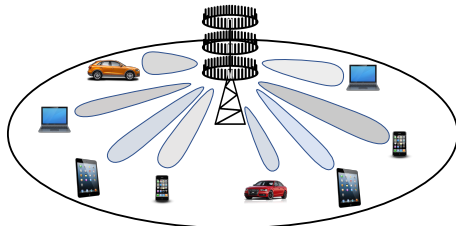


Figure: Cellular base-station with a large-scale antenna array

- **Time-Division Duplex (TDD) Massive MIMO:**
 - Channel reciprocity can be assumed.
 - Uplink pilot transmission followed by CSI estimation at BS and downlink transmission.
- **Frequency-Division Duplex (FDD) Massive MIMO:**
 - Channel reciprocity does not necessarily hold in different frequencies.
 - Downlink pilot transmission followed by CSI estimation and feedback at the users.

Channel Estimation, Feedback and Precoding in FDD Massive MIMO

Conventional downlink FDD wireless system design involves:

- Independent **channel estimation** at each UE based on downlink pilot.
- Independent **quantization** and **feedback** of each user's channel to the BS.
- Multiuser **precoding** at the BS based on channel feedback from ALL the users.

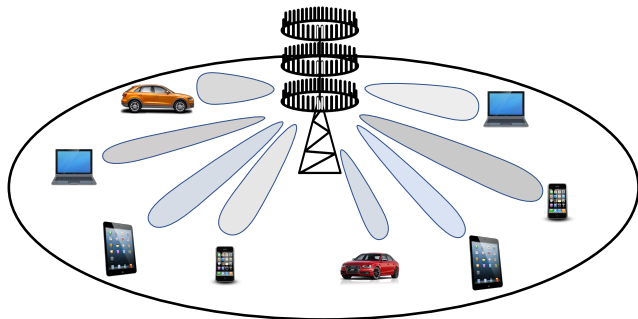
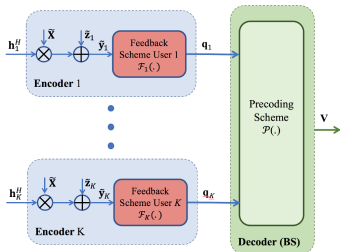
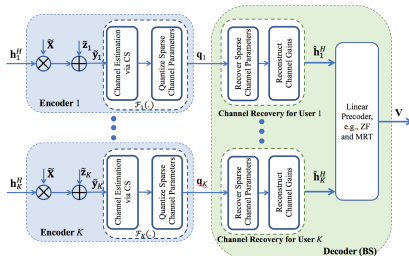


Figure: Cellular base-station with a large-scale antenna array

Single-user channel feedback for multiuser precoding is NOT optimal.



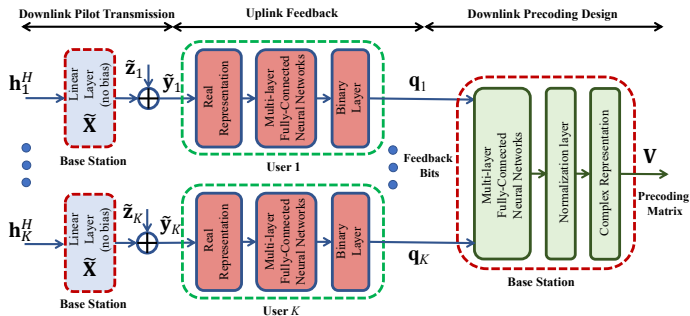
FDD downlink precoding as a DSC problem.



The conventional scheme amounts to a separate source coding strategy.

- The FDD feedback/precoding problem is a distributed source coding (DSC) problem.
- Much more efficient distributed feedback scheme can be designed using machine learning.

Graph Neural Network for Distributed Channel Estimation and Compression



- **Downlink Pilot Transmission:** Modelled by a linear neural layer followed by additive noise.
- **Uplink Feedback:** Modelled by an R -layer DNN with B binary activation neurons at the last layer: $\mathbf{q}_k = \text{sgn} \left(\mathbf{W}_R^{(k)} \sigma_{R-1} \left(\cdots \sigma_1 \left(\mathbf{W}_1^{(k)} \tilde{\mathbf{y}}_k + \mathbf{b}_1^{(k)} \right) \cdots \right) + \mathbf{b}_R^{(k)} \right)$.
- **Downlink Precoding Design:** Modelled by a T -layer DNN with normalization activation function at the last layer: $\mathbf{v} = \tilde{\sigma}_T \left(\tilde{\mathbf{W}}_T \tilde{\sigma}_{T-1} \left(\cdots \tilde{\sigma}_1 \left(\tilde{\mathbf{W}}_1 \mathbf{q} + \tilde{\mathbf{b}}_1 \right) + \cdots \right) + \tilde{\mathbf{b}}_T \right)$.
- Sum rate maximization can be cast as the following learning problem:

$$\tilde{\mathbf{x}}, \left\{ \mathbf{e}_R^{(k)} \right\}, \Theta_T \max_{\tilde{\mathbf{x}}, \left\{ \mathbf{e}_R^{(k)} \right\}, \Theta_T} \mathbb{E}_{\mathbf{H}, \tilde{\mathbf{z}}} \left[\sum_k \log_2 \left(1 + \frac{|\mathbf{h}_k^H \mathbf{v}_k|^2}{\sum_{j \neq k} |\mathbf{h}_k^H \mathbf{v}_j|^2 + \sigma^2} \right) \right], \quad (1)$$

Numerical Results: FDD Massive MIMO System with UE Feedback

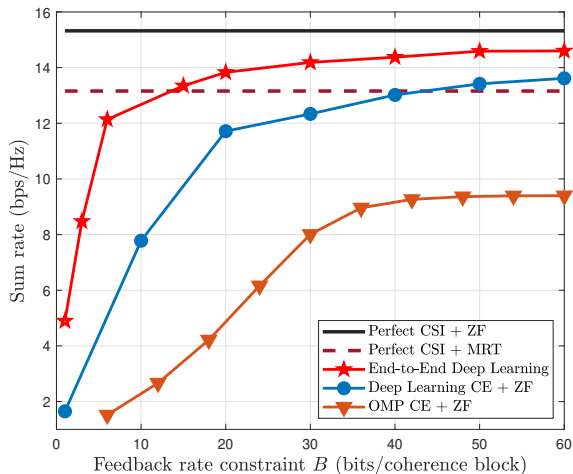


Figure: Sum rate achieved by different methods in a 2-user FDD system with number of BS antennas $M = 64$, Pilot length $L = 8$, number of paths $L_p = 2$, number of users $K = 2$, and $\text{SNR} \triangleq 10 \log_{10}(\frac{P}{\sigma^2}) = 10\text{dB}$.

Active Sensing via Learning

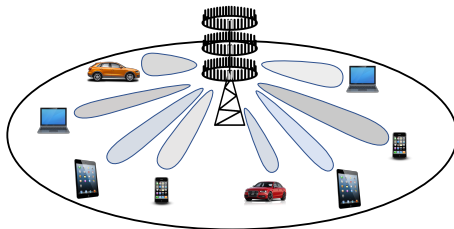
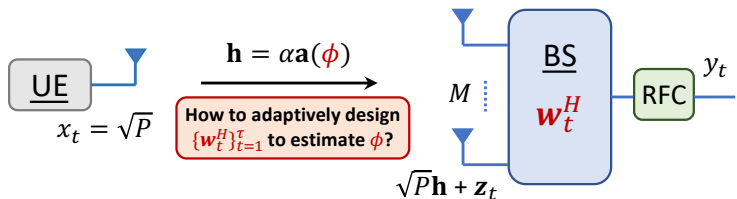


Figure: Cellular base-station with a large-scale antenna array.

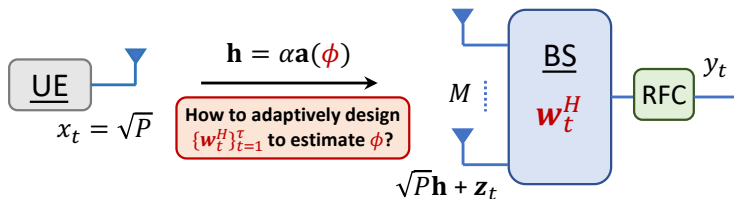
- Motivation: mmWave massive MIMO for enhanced mobile broadband.
- Estimating high-dimensional channel from low-dimensional observations is challenging:
 - Fully digital beamforming: Requires one high-resolution RF chain per antenna element.
 - Hybrid beamforming: Analog beamformer with low-dimensional digital beamforming.
- **Initial Beam Alignment:** How to find channel direction in an RF chain limited system?

Sensing Architecture with Hybrid Beamforming



- A BS with M antennas and a single RF chain serves a single-antenna user
- The user transmits pilot; the BS tries to estimate the channel.

Sensing Architecture with Hybrid Beamforming



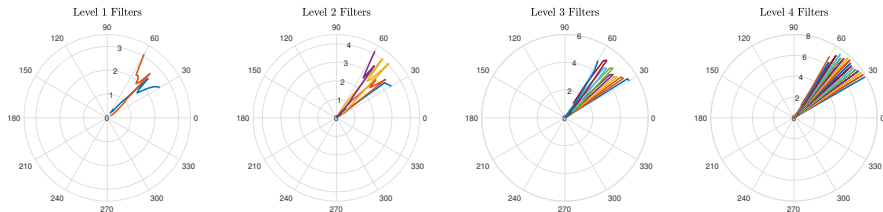
- A BS with M antennas and a single RF chain serves a single-antenna user
- The user transmits pilot; the BS tries to estimate the channel.
- Due to the RF chain limitation, the BS must sense the channel through analog combiners:

$$y_t = \mathbf{w}_t^H \mathbf{h} x_t + \mathbf{w}_t^H \mathbf{z}_t = \sqrt{P} \alpha \mathbf{w}_t^H \mathbf{a}(\phi) + n_t, \quad (2)$$

- \mathbf{w}_t is the sensing (combining) vector in time frame t with $\|\mathbf{w}_t\|^2 = 1$
- $\alpha \sim \mathcal{CN}(0, 1)$ is the fading coefficient,
- $\phi \in [\phi_{\min}, \phi_{\max}]$ is the angle of arrival (AoA),
- $\mathbf{a}(\phi) = [1, e^{j\pi \sin \phi}, \dots, e^{j(M-1)\pi \sin \phi}]^T$ is the array response vector,
- $n_t \sim \mathcal{CN}(0, 1)$ is the effective noise.

Traditional Approach: Bisection in Angle Domain

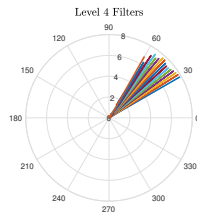
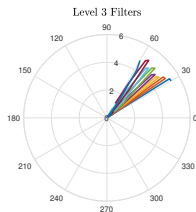
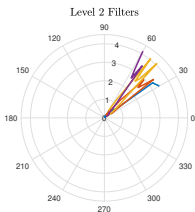
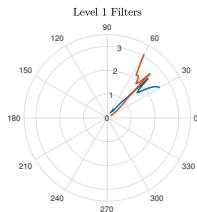
- We can select the sensing vector from a pre-designed codebook that minimizes the expected MSE objective, e.g., the codebook contains the following 30 filters bisecting in angle domain.



- Hierarchical beamforming codebook [Alkhateeb, Ayach, Leus, and Heath, 2014].

Traditional Approach: Bisection in Angle Domain

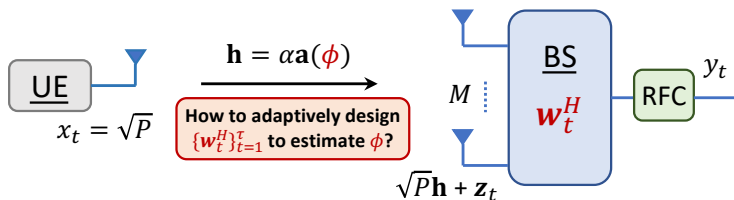
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... but bisection can be sensitive to noise.

Initial Alignment as a Sequential Decision Problem



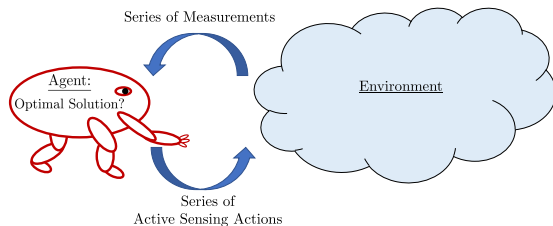
- **Initial Beam Alignment:** The BS can optimize the quality of AoA estimation by designing \mathbf{w}_t at each time frame, possibly sequentially in an adaptive manner, i.e.,

$$\mathbf{w}_{t+1} = \tilde{\mathcal{G}}_t(y_{1:t}, \mathbf{w}_{1:t}), \quad \forall t \in \{0, \dots, T-1\}. \quad (3)$$

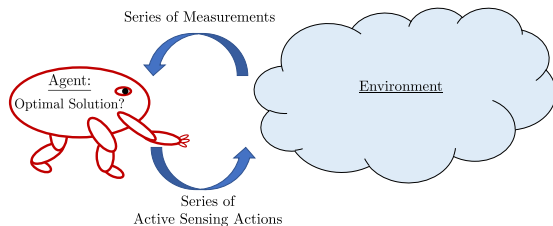
- The final AoA estimate is obtained as a function of all past observations as:

$$\hat{\phi} = \tilde{\mathcal{F}}(y_{1:T}, \mathbf{w}_{1:T}). \quad (4)$$

- The goal is to design $\mathbf{w}_{1:T}$ sequentially as function of $y_{1:T}$ so far to minimize $\mathbb{E} \left[\left(\hat{\phi} - \phi \right)^2 \right]$.
- This is a high-dimensional sequential decision problem!



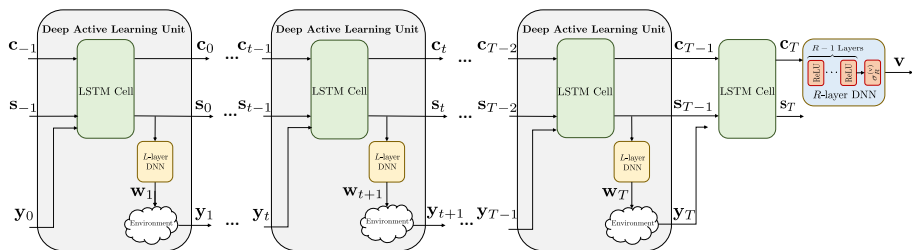
- The active sequential learning problem naturally arises in many inference, sensing, and control settings, e.g., tree-search, sequential design of experiments, the multi-armed bandit.
- Problems involve adaptive estimation/control based on sequential sensing of environment.
- Analytic solutions seem impossible.
- Numerical solutions are computationally complex and in general hard to obtain.



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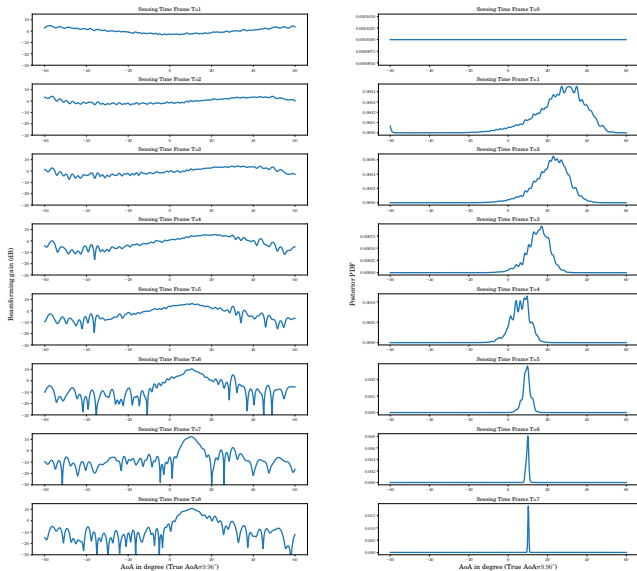
How about using machine learning to find a solution efficiently?

Long Short-Term Memory (LSTM) Architecture for Deep Active Sensing



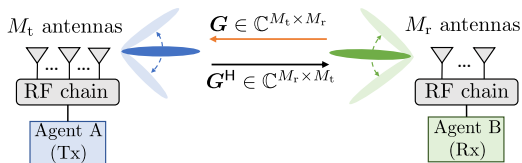
- We use a recurrent neural network with LSTM cells to model the active sensing problem.
- The overall end-to-end sensing architecture is a very deep neural network.
- We train the overall DNN by using stochastic gradient descent to minimize the MSE.

Posterior Distribution of AoA and Optimized Sensing Vectors



Two-Sided Beam Alignment

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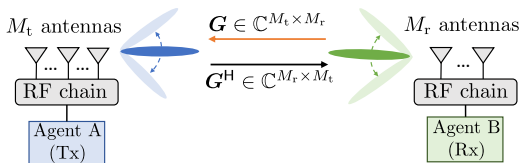


- Received signal at the Rx

$$r = \mathbf{w}_r^H \mathbf{G}^H \mathbf{w}_t x + n, \quad (5)$$

- $x \in \mathbb{C}$ is the intended data symbol with $\mathbb{E}[|x|^2] = P$.
- $\mathbf{w}_t \in \mathbb{C}^{M_t}$ is the beamforming vectors at the Tx with $\|\mathbf{w}_t\|_2 = 1$.
- $\mathbf{w}_r \in \mathbb{C}^{M_r}$ is the beamforming vectors at the Rx with $\|\mathbf{w}_r\|_2 = 1$.
- $n \sim \mathcal{CN}(0, \sigma_0^2)$ is the additive Gaussian noise.
- Goal:** Aligning the beams $\{\mathbf{w}_t, \mathbf{w}_r\}$ to maximize the beamforming gain $|\mathbf{w}_r^H \mathbf{G}^H \mathbf{w}_t|^2$.

Two-Sided Beam Alignment



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- Goal:** Aligning the beams $\{\mathbf{w}_t, \mathbf{w}_r\}$ to maximize the beamforming gain $|\mathbf{w}_r^H \mathbf{G}^H \mathbf{w}_t|^2$.
- Given perfect CSI \mathbf{G} , the optimal beamforming vectors are

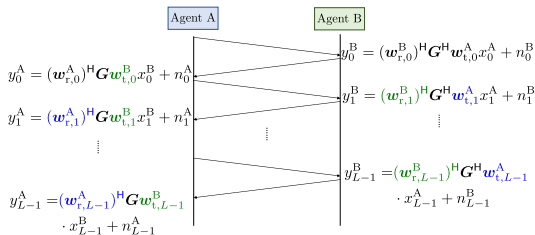
$$\mathbf{w}_t^* = \mathbf{u}_{\max} / \|\mathbf{u}_{\max}\|_2, \quad (6a)$$

$$\mathbf{w}_r^* = \mathbf{v}_{\max} / \|\mathbf{v}_{\max}\|_2, \quad (6b)$$

Here, \mathbf{u}_{\max} and \mathbf{v}_{\max} are respectively the left and the right singular vectors associated with the largest singular value of the matrix \mathbf{G} .

Ping-Pong Pilot Protocol

We propose an active learning framework with ping-pong pilot transmission.



In the ℓ -th transmission round:

- Agent A sends a pilot x_ℓ^A to agent B:

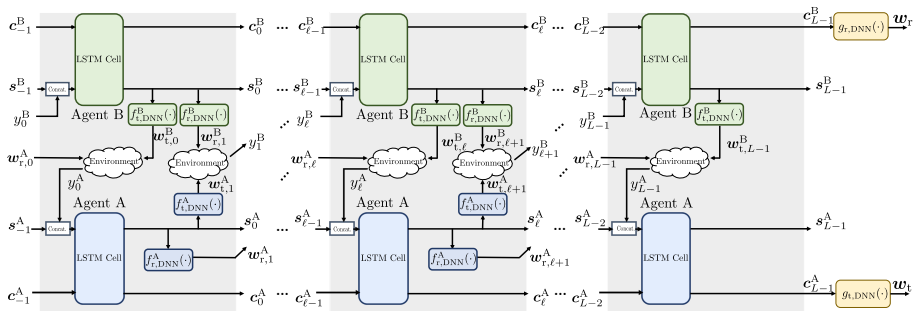
$$y_\ell^B = (\mathbf{w}_{r,\ell}^B)^H \mathbf{G}^H \mathbf{w}_{t,\ell}^A x_\ell^A + n_\ell^B, \quad \ell = 0, \dots, L-1, \quad (7)$$

- Agent B sends back a pilot x_ℓ^B to agent A:

$$y_\ell^A = (\mathbf{w}_{r,\ell}^A)^H \mathbf{G} \mathbf{w}_{t,\ell}^B x_\ell^B + n_\ell^A, \quad \ell = 0, \dots, L-1, \quad (8)$$

After L rounds of pilot transmission, each of the transceivers obtains L measurements of the channel, which can be utilized to design their own data transmission beamforming vectors.

Deep Active Sensing



Agents A and B respectively utilize the historical $\{y_i^A\}_{i=0}^{\ell}$ and $\{y_i^B\}_{i=0}^{\ell}$ to design their transmit/receive sensing beamformers:

$$w_{t,\ell+1}^A = f_{t,\ell}^A(\{y_i^A\}_{i=0}^{\ell}), \quad w_{r,\ell+1}^A = f_{r,\ell}^A(\{y_i^A\}_{i=0}^{\ell}), \quad (9)$$

$$w_{t,\ell}^B = f_{t,\ell}^B(\{y_i^B\}_{i=0}^{\ell}), \quad w_{r,\ell+1}^B = f_{r,\ell}^B(\{y_i^B\}_{i=0}^{\ell}), \quad (10)$$

After L rounds of pilot transmission, the beamformers for data transmission are designed as:

$$w_t = g_t(\{y_i^A\}_{i=0}^{L-1}), \quad w_r = g_r(\{y_i^B\}_{i=0}^{L-1}), \quad (11)$$

The overall objective is to maximize $\mathbb{E} [|w_r^H G^H w_t|^2]$.

Interpretation of Learned Active Sensing Strategy

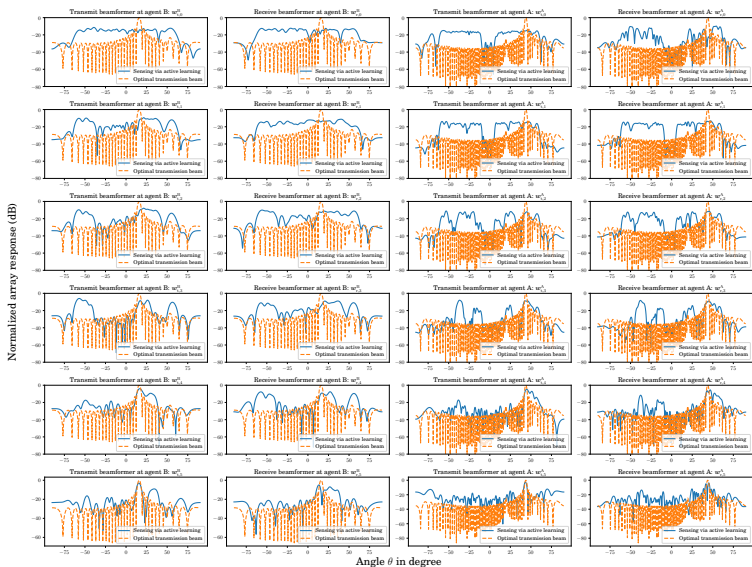
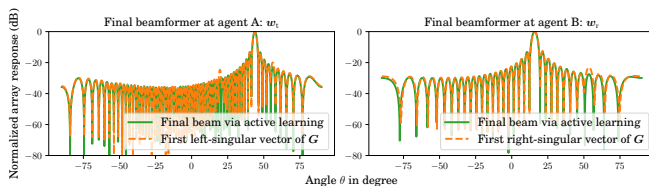
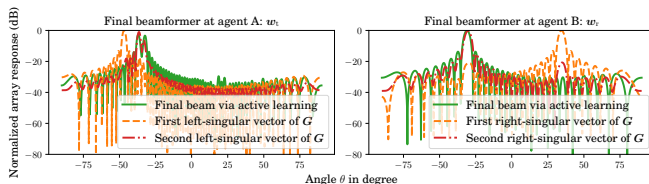


Figure: Learned sensing beamforming patterns for a specific mmWave channel realization.

Singular Value Decomposition Over the Air



(a) Example of beamformers matching the strongest singular-vector direction



(b) Example of beamformers matching the second singular-vector direction

Figure: Two examples of learned **data transmission** nbeamforming patterns after 6 ping-pong pilots.

Performance on Ray-Tracing Channel Model

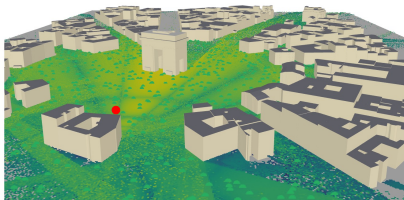


Figure: Ray-tracing model.

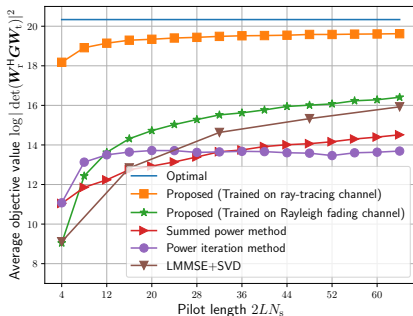


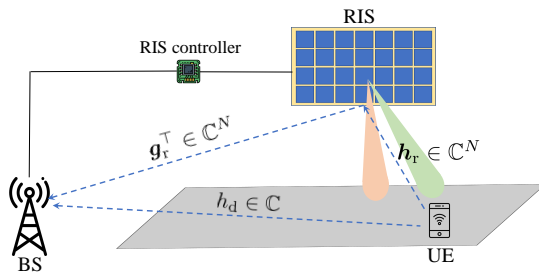
Figure: $M_t = 64$, $M_r = 16$ and $N_s = 2$.

- The model trained with site-specific ray-tracing channel achieves the best performance.
- The model trained with Rayleigh fading channel can generalize to the ray-tracing scenario.
- Here, we assume fully digital system with two data streams, trained using GRU.

Localization and Beam Tracking

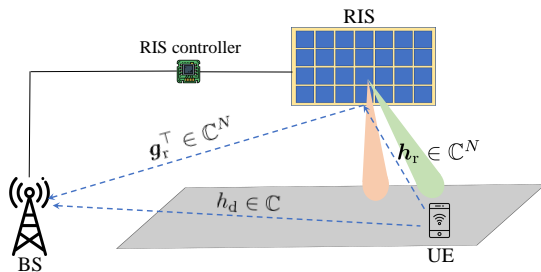
RIS-Assisted Active Uplink Localization

- A single user (UE) repeatedly transmits pilot symbols
- The base station (BS) receives the pilots through reflection by the RIS
- The BS determines the location of the user based on the received pilots



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The idea is to adaptively configure the RIS:

- The uplink RIS configurations are sequentially designed by the BS as a function of previous measurements to minimize localization error.
- As a result, the RIS can focus the beam progressively to locate the user over time as more measurements become available.

- The goal is to estimate the unknown UE position \mathbf{p} based on T observations $\{y_t(\boldsymbol{\theta}_t)\}_{t=0}^{T-1}$.
- The design of RIS configuration is a function of historical measurements.
- The estimated UE position $\hat{\mathbf{p}}$ is a function of all T historical observations.

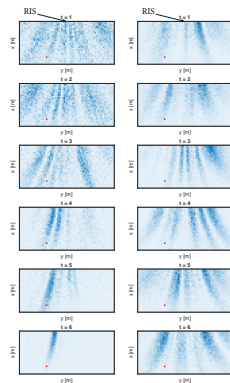
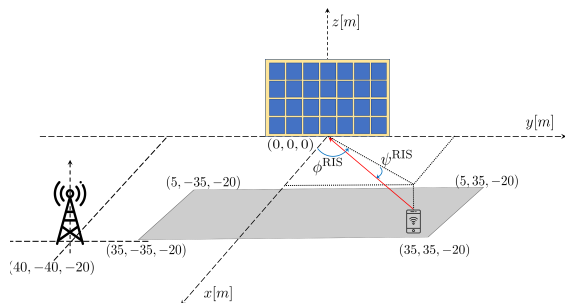
$$\begin{aligned} & \underset{\{q_t(\cdot)\}_{t=0}^{T-1}, f(\cdot)}{\text{minimize}} && \mathbb{E} [\|\hat{\mathbf{p}} - \mathbf{p}\|_2^2] \\ & \text{subject to} && \|\boldsymbol{\theta}_t\|_n = 1, \forall n, t, \\ & && \boldsymbol{\theta}_{t+1} = q_t(\{y_\tau\}_{\tau=0}^t), \quad t = 0, \dots, T-1, \\ & && \hat{\mathbf{p}} = f(\{y_t\}_{t=0}^{T-1}). \end{aligned}$$

- The problem amounts to optimizing the functions $\{q_t(\cdot)\}_{t=0}^{T-1}$ and $f(\cdot)$.

Proposal:

- To use an LSTM network to automatically construct state vectors from the historical measurements and to extract temporal features and long-term dependencies in these observations to facilitate the design of reflection coefficients.

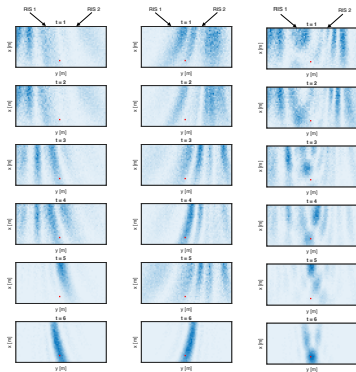
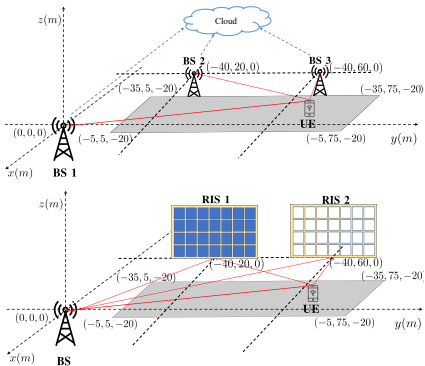
Single-RIS for Localization



- The BS is located at $\mathbf{p}^{\text{BS}} = (40\text{m}, -40\text{m}, -20\text{m})$
- An 8×8 RIS is located at $\mathbf{p}^{\text{RIS}} = (0\text{m}, 0\text{m}, 0\text{m})$
- The unknown user locations \mathbf{p} are uniformly generated within a rectangular area on the x - y plane $(20 \pm 15\text{m}, 0 \pm 35\text{m}, -20\text{m})$.
- Diagram shows the beamforming patterns of active sensing (left) vs. non-active (right)

Multiple RISs for Triangulation

- Localization becomes more accurate if multiple anchor points are deployed.
- Instead of deploying extra base-stations, a more cost-effective solution is to use RISs.



The RIS reflection patterns of left panel, right panel, and combined patterns are shown.

Pilot Transmission Phase

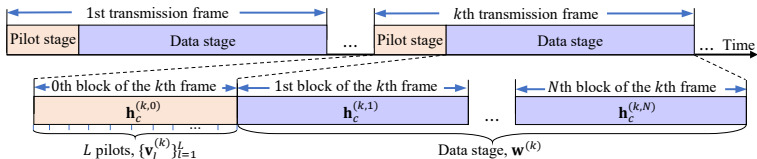


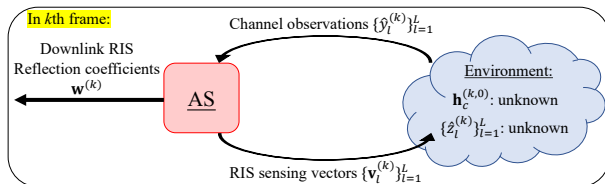
Figure: Frame structure of the proposed transmission protocol.

- The time-varying channels are split into sufficiently small fixed-length blocks:
 - The channels within each block is assumed to remain constant;
 - The channels are **correlated** across the blocks due to the mobility of the UE.
- The ℓ th pilot received by the AP in the pilot stage (0th block) of the k th frame:

$$\hat{y}_\ell^{(k)} = \left(\mathbf{h}_t^{(k,0)} \right)^\top \text{diag} \left(\mathbf{v}_\ell^{(k)} \right) \mathbf{h}_r^{(k,0)} x_\ell^{(k)} + \hat{z}_\ell^{(k)} = \sqrt{P_u} \left(\mathbf{v}_\ell^{(k)} \right)^\top \mathbf{h}_c^{(k,0)} + \hat{z}_\ell^{(k)}, \quad (13)$$

- The ℓ th RIS **sensing vector** for in the k th frame: $\mathbf{v}_\ell^{(k)} = [e^{j\theta_1}, \dots, e^{j\theta_{N_r}}]^\top$ with $\theta_i \in [0, 2\pi)$.
- $\mathbf{h}_c^{(k,0)} \triangleq \text{diag}(\mathbf{h}_t^{(k,0)})\mathbf{h}_r^{(k,0)} \in \mathbb{C}^{N_r}$ is the cascaded channel in the 0th block of the k th frame.
- The idea is to exploit the temporal channel correlation by designing the best sensing vector \mathbf{v} .

Update the RIS configurations for both sensing and communications in a sequential fashion.



- In the pilot stage of the k th frame, the RIS sensing vectors are designed as:

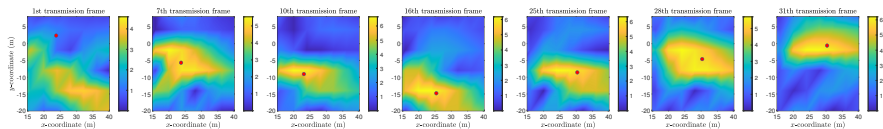
$$\{\mathbf{v}_\ell^{(k)}\}_{\ell=1}^L = \mathcal{G}^{(k)} \left(\left\{ \{\hat{\mathbf{y}}_\ell^{(j)}\}_{\ell=1}^L \right\}_{j=1}^{k-1}, \left\{ \{\mathbf{v}_\ell^{(j)}\}_{\ell=1}^L \right\}_{j=1}^{k-1} \right) \quad (14)$$

- $\mathcal{G}^{(k)} : \mathbb{C}^{L(k-1)} \times \mathbb{C}^{N_r L(k-1)} \rightarrow \mathbb{C}^{N_r L}$ is the active sensing scheme in the k th frame.
- Using the newly received pilots, design $\mathbf{w}^{(k)}$ for the N blocks in the subsequent data frame:

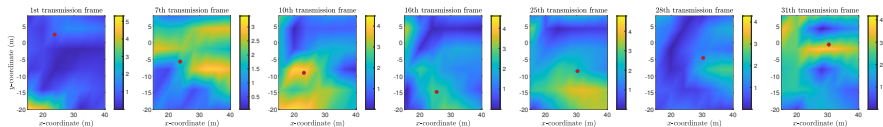
$$\mathbf{w}^{(k)} = \mathcal{F}^{(k)} \left(\left\{ \{\hat{\mathbf{y}}_l^{(j)}\}_{l=1}^L \right\}_{j=1}^k, \left\{ \{\mathbf{v}_l^{(j)}\}_{l=1}^L \right\}_{j=1}^k \right) \quad (15)$$

- $\mathcal{F}^{(k)} : \mathbb{C}^{Lk} \times \mathbb{C}^{N_r Lk} \rightarrow \mathbb{C}^{N_r}$ is the downlink alignment scheme in the k th frame.
- Goal: Maximizing the downlink data rate

Visualizing Downlink RIS Reflection Coefficients



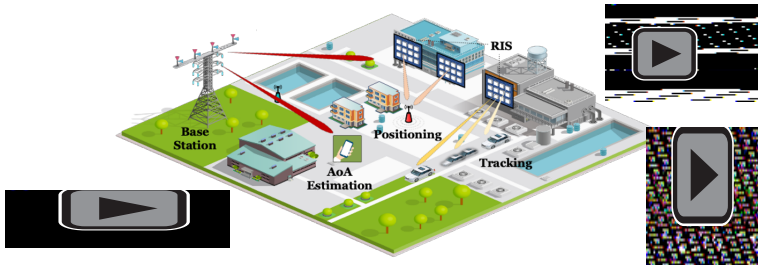
(a) Proposed active sensing approach using LSTM



(b) DNN-based benchmark (fixed sensing vector learned from channel statistics)

Figure: Instantaneous downlink rate around the position of the UE obtained in different transmission frames. UE transmits $L = 10$ pilots in each pilot stage, each frame contains $N = 30$ blocks, $P_u = P_d = 15\text{dBm}$, $N_r = 64$.

- Machine learning enables a data-driven approach for communications and sensing tasks:
 - Data-driven design of massive MIMO beamformers *without* explicit channel estimation.
 - Data-driven design of active sensing strategies for beam alignment, beam tracking, and localization.
- Designing neural network architecture to fit the problem structure is the key to success.
 - GNN is able to capture the spatial relationship of the BS, the RIS, and the mobile users.
 - LSTM network is able to capture the temporal correlations across multiple sensing stages and to track the time-varying nature of the channel by summarizing the state of the system.



Data-Drive Methods are the Future of Optimization!



Wei Yu, Foad Sohrabi, and Tao Jiang, "Role of Machine Learning in Wireless Communications", *IEEE BITS the Information Theory Magazine*, vol.2, no.2, pp.56-72, November 2022.



Foad Sohrabi, Kareem M. Attiah, Wei Yu, "Deep Learning for Distributed Channel Feedback and Multiuser Precoding in FDD Massive MIMO", *IEEE Transactions on Wireless Communications*, vol. 20, no. 7, pp. 4044-4057, July 2021.



Foad Sohrabi, Tao Jiang, Wei Cui, and Wei Yu, "Active Sensing for Communications by Learning", *IEEE Journal on Selected Areas in Communications*, vol.40, no.6, pp.1780-1794, June 2022.



Tao Jiang, Foad Sohrabi, Wei Yu, "Active Learning for Two-Sided Beam Alignment and Reflection Design Using Ping-Pong Pilots", *IEEE Journal on Selected Areas in Information Theory*, May 15, 2023.



Zhongze (David) Zhang, Tao Jiang, and Wei Yu, "Localization with Reconfigurable Intelligent Surface: An Active Sensing Approach", *IEEE Transactions on Wireless Communications*, To appear in 2024.



Han Han, Tao Jiang, and Wei Yu, "Active Beam Tracking with Reconfigurable Intelligent Surface", *IEEE Conference on Speech, Acoustics, and Signal Processing (ICASSP)*, June 2023.